$\qquad$

## Source of Charge

- An atom
$\qquad$
- Protons - $\qquad$ charge
- Neutrons - $\qquad$ charge, but same $\qquad$ as proton
- Electron cloud
- Electron - $\qquad$ charge, $\qquad$ mass
- $q_{e}=-1.60 \times 10^{-19} \mathrm{C}$
- Unit of charge: $\qquad$ (C)
- $q_{e}$ is the $\qquad$ charge discovered
- Electricity is $\qquad$ $\rightarrow$ comes in $\qquad$ numbers
- $\quad\left|q_{e}\right|$ is the $\qquad$ unit of charge
- In nature atoms have $\qquad$ net charge
- \# $\qquad$ = \# $\qquad$
How many electrons does it take to make a charge of $-4 \times 10^{-6} \mathrm{C}$ ? What is their mass $\left(m_{e}=9.11 \times 10^{-31} \mathrm{~kg}\right)$ ?


## Law of Conservation of Charge

During any process, the net
of $a$ $\qquad$ system remains $\qquad$

- Like charges $\qquad$
- Unlike charges $\qquad$
- The attraction and repulsion are $\qquad$ and can be used with $\qquad$ Laws and other dynamics problems


## Conductors and Insulators

- Electricity can flow $\qquad$ objects
- Conductors let electrons flow
- Most $\qquad$ conductors are also $\qquad$ conductors
- $\qquad$
- Insulators are very poor conductors


## Charging by contact

- Negative charged rod gives some $\qquad$ to sphere
- Sphere becomes $\qquad$ charged until charges are $\qquad$


## Charging by Induction

- Charge without $\qquad$
- Charged rod comes near $\qquad$ sphere
- The like charges are $\qquad$ to
$\qquad$ side of sphere
- A $\qquad$ wire lets the charges
$\qquad$ from the sphere
- The $\qquad$ wire is $\qquad$ , then

(a)

(b)
 the charged rod
- Sphere is $\qquad$
$\qquad$
- If the sphere was $\qquad$ instead of metal
- Electrons $\qquad$ flow
- The surface would become $\qquad$ charged as the electrons in each individual atom rearrange, but no
$\qquad$ effect
○ $\qquad$ cling is made by this $\qquad$


## Homework

1. There are very large numbers of charged particles in most objects. Why, then, don't most objects exhibit static electricity?
2. An eccentric inventor attempts to levitate by first placing a large negative charge on himself and then putting a large positive charge on the ceiling of his workshop. Instead, while attempting to place a large negative charge on himself, his clothes fly off. Explain.
3. When a glass rod is rubbed with silk, it becomes positive and the silk becomes negative-yet both attract dust. Does the dust have a third type of charge that is attracted to both positive and negative? Explain.
4. Describe how a positively charged object can be used to give another object a negative charge. What is the name of this process?
5. What is grounding? What effect does it have on a charged conductor? On a charged insulator?
6. A metallic object is given a positive charge by induction. (a) Does the mass of the object increase, decrease, or remain the same? Why? (b) What happens to the mass of the object if it is given a negative charge by induction?
7. Common static electricity involves charges ranging from nanocoulombs to microcoulombs. (a) How many electrons are needed to form a charge of -2.00 nC (b) How many electrons must be removed from a neutral object to leave a net charge

8. If $1.80 \times 10^{20}$ electrons move through a pocket calculator during a full day's operation, how many coulombs of charge moved through it? (OpenStax 18.2) -28.8 C
9. To start a car engine, the car battery moves $3.75 \times 10^{21}$ electrons through the starter motor. How many coulombs of charge were moved? (OpenStax 18.3) -600 C
10. A certain lightning bolt moves 40.0 C of charge. How many fundamental units of charge $\left|q_{e}\right|$ is this? (OpenStax 18.4) $2.50 \times 10^{20}$
11. Suppose a speck of dust in an electrostatic precipitator has $1.0000 \times 10^{12}$ protons in it and has a net charge of -5.00 nC (a very large charge for a small speck). How many electrons does it have? (OpenStax 18.5) $\mathbf{1 . 0 3} \times \mathbf{1 0}^{\mathbf{1 2}}$
12. An amoeba has $1.00 \times 10^{16}$ protons and a net charge of 0.300 pC . (a) How many fewer electrons are there than protons? (b) If you paired them up, what fraction of the protons would have no electrons? (OpenStax 18.6) $\mathbf{1 . 8 8} \times \mathbf{1 0}^{\mathbf{6}}, \mathbf{1 . 8 8} \times$ $10^{-10}$
13. Consider three identical metal spheres, A, B, and C. Sphere A carries a charge of $+5 q$. Sphere $B$ carries a charge of $-q$. Sphere C carries no net charge. Spheres A and B are touched together and then separated. Sphere C is then touched to sphere A and separated from it. Last, sphere C is touched to sphere B and separated from it. (a) How much charge ends up on sphere C? What is the total charge on the three spheres (b) before they are allowed to touch each other and (c) after they have touched? (Cutnell 18.5) 1.5q, 4q, 4q
$\qquad$

## Coulomb's Law

- $\qquad$ charges exert $\qquad$ on each other
- Related to the $\qquad$ of the charges and the $\qquad$ between them
- If the signs are $\qquad$ force $\qquad$
- If the signs are $\qquad$ force $\qquad$
Coulomb's Law

$$
F=k \frac{\left|q_{1} q_{2}\right|}{r^{2}}
$$

Where $F=$ electrostatic force, $k=$ constant $\left(8.99 \times 10^{9} \mathrm{Nm}^{2} / C^{2}\right), q=$ charge, $r=$ distance between the charges
In a hydrogen atom, the electron $\left(q=-1.60 \times 10^{-19} \mathrm{C}\right)$ is $5.29 \times 10^{-11} \mathrm{~m}$ away from the proton of equal charge magnitude. Find the electrical force of attraction.

## Force on 1 charge by 2 others

- Work in $\qquad$ of attraction by $\qquad$ of the points
- Find $\qquad$ of attraction by the $\qquad$ point
- Find $\qquad$
- Add the force $\qquad$
- REMEMBER!!!!! You have to add the $\qquad$ and $\qquad$ !!!!!

There are three charges in a straight line: $q_{1}=+2 \mu C$ at $x=-0.1 \mathrm{~m}, q_{2}=-3 \mu C$ at $\mathrm{x}=0 \mathrm{~m}, q_{3}=+5 \mu C$ at $\mathrm{x}=0.3 \mathrm{~m}$. What is the force on $q_{2}$ ?

There are three charges: $q_{1}=+2 \mu C$ at $(0,0.3) \mathrm{m}, q_{2}=-3 \mu C$ at $(0,0) \mathrm{m}, q_{3}=+5 \mu C$ at $(0.1,0.2) \mathrm{m}$. What is the force on $q_{2}$ ?

## Homework

1. The figure shows the charge distribution in a water molecule, which is called a polar molecule because it has an inherent separation of charge. Given water's polar character, explain what effect humidity has on removing excess charge from objects.
2. A proton and an electron are held in place on the $x$ axis. The proton is at $x=-d$, while the electron is at $x=+d$. They are released simultaneously, and the only force that affects their motions is the electrostatic force of attraction that each applies to the other. Which particle reaches the origin first? Give your reasoning.
3. Identical point charges are fixed to opposite corners of a square. Where does a third point charge experience the greater net force, at one of the empty corners or at the center of the square? Account for your answer.
4. What is the repulsive force between two pith balls that are 8.00 cm apart and have equal charges of -30.0 nC ? (OpenStax 18.10) $\mathbf{1 . 2 7 \times 1 0} \mathbf{1 0}^{\mathbf{- 3}} \mathrm{N}$
5. (a) How strong is the attractive force between a glass rod with a $0.700 \mu \mathrm{C}$ charge and a silk cloth with a $-0.600 \mu \mathrm{C}$ charge, which are 12.0 cm apart, using the approximation that they act like point charges? (b) Discuss how the answer to this problem might be affected if the charges are distributed over some area and do not act like point charges. (OpenStax 18.11) $\mathbf{0 . 2 6 3} \mathbf{N}$
6. Two point charges exert a 5.00 N force on each other. What will the force become if the distance between them is increased by a factor of three? (OpenStax 18.12) $0.556 \mathbf{N}$
7. Two point charges are brought closer together, increasing the force between them by a factor of 25 . By what factor was their separation decreased? (OpenStax 18.13) 5 times
8. How far apart must two point charges of 75.0 nC (typical of static electricity) be to have a force of 1.00 N between them? (OpenStax 18.14) 7.12 mm
9. If two equal charges each of 1 C each are separated in air by a distance of 1 km , what is the magnitude of the force acting between them? You will see that even at a distance as large as 1 km , the repulsive force is substantial because 1 C is a very significant amount of charge. (OpenStax 18.15) $\mathbf{9} \times \mathbf{1 0}^{\mathbf{3}} \mathbf{N}$
10. A test charge of $+2 \mu \mathrm{C}$ is placed halfway between a charge of $+6 \mu \mathrm{C}$ and another of $+4 \mu \mathrm{C}$ separated by 10 cm . (a) What is the magnitude of the force on the test charge? (b) What is the direction of this force (away from or toward the $+6 \mu \mathrm{C}$ charge)? (OpenStax 18.16) $\mathbf{1 0} \mathrm{N}$, away from the $\mathbf{6} \mu \mathrm{C}$ charge
11. Bare free charges do not remain stationary when close together. To illustrate this, calculate the acceleration of two isolated protons separated by 2.00 nm (a typical distance between gas atoms). (OpenStax 18.17) $\mathbf{3 . 4 5 \times 1 0} \mathbf{1 6} \mathbf{~ m} / \mathbf{s}^{\mathbf{2}}$
12. (a) Find the ratio of the electrostatic to gravitational force between two electrons. (b) What is this ratio for two protons? (c) Why is the ratio different for electrons and protons? (OpenStax 18.21) $\mathbf{4 . 1 6 \times \mathbf { 1 0 } ^ { \mathbf { 4 2 } } , \mathbf { 1 . 2 4 } \times \mathbf { 1 0 } ^ { \mathbf { 3 6 } } , ~ ( 0 )}$
$\qquad$

## Electric Field

- We can use a $\qquad$ charge to determine how the surrounding $\qquad$ generate a $\qquad$
- Pick a small test charge so it doesn't $\qquad$ the surrounding charge $\qquad$
A test charge ( $q_{0}=1.0 \times 10^{-10} \mathrm{C}$ ) experiences a force of $2 \times 10^{-9} \mathrm{~N}$ when placed near a charged sphere. Determine the Force per Coulomb that the charge experiences and predict the force on a $2 C$ charge.


## Electric Field Definition

$$
E=\frac{F}{q_{0}}=\frac{k q}{r^{2}}
$$

- per $\qquad$
- Vector
- Same $\qquad$ as the force on a $\qquad$ test charge
- Unit: N/C

There is a point charge of $q=2 \times 10^{-8} C$. Determine the E-field at 0.50 m away using a test charge of $1 \times 10^{-10} \mathrm{C}$.

There are two point charges of $q_{1}=4 C$ and $q_{2}=8 C$ and they are 10 m apart. Find point where $E=0$ between them.

## Electric Field Lines

- Map to show the $\qquad$ in $\qquad$
- Rules
- Lines begin at $\qquad$ charges only
- Lines end at $\qquad$ charges only
- The number of lines entering or leaving a charge is $\qquad$ to the $\qquad$ of charge
- Lines don't $\qquad$ each other
- Lines leave surfaces at $\qquad$ degrees



## What is wrong here?



## Homework

1. Why must the test charge $\mathrm{q}_{0}$ in the definition of the electric field be vanishingly small?
2. The figure shows an electric field extending over three regions, labeled I, II, and III. Answer the following questions. (a) Are there any isolated charges? If so, in what region and what are their signs? (b) Where is the field strongest? (c) Where is it weakest? (d) Where is the field the most uniform?
3. There is an electric field at point P. A very small charge is placed at this point and experiences a force. Another very small charge is then placed at this point and experiences a force that differs in both magnitude and direction from that experienced by the first
 charge. How can these two different forces result from the single electric field that exists at point P?
4. Drawings I and II show two examples of electric field lines. Decide which of the following statements are true and which are false, defending your choice in each case. (a) In both I and II the electric field is the same everywhere. (b) As you move from left to right in each case, the electric field becomes stronger. (c) The electric field in I is the same everywhere but becomes stronger in II as you move from left to right. (d) The electric fields in both I and II could be created by negative charges located somewhere on the left and positive charges somewhere on the right. (e) Both I and II arise from a single positive point charge located somewhere on the left.

5. What is the magnitude and direction of an electric field that exerts a $2.00 \times 10^{-5} \mathrm{~N}$ upward force on a $-1.75 \mu \mathrm{C}$ charge? (OpenStax 18.27) -11.4 N/C downward
6. What is the magnitude and direction of the force exerted on a $3.50 \mu \mathrm{C}$ charge by a $250 \mathrm{~N} / \mathrm{C}$ electric field that points due east? (OpenStax 18.28) 8.75 $\times \mathbf{1 0}^{-\mathbf{4}} \mathrm{N}$
7. Calculate the magnitude of the electric field 2.00 m from a point charge of 5.00 mC (such as found on the terminal of a Van de Graaff). (OpenStax 18.29) $\mathbf{1 . 1 3 \times 1 0 { } ^ { \mathbf { 7 } } \mathbf { ~ N } / \mathrm { C } , ~}$
8. (a) What magnitude point charge creates a $10,000 \mathrm{~N} / \mathrm{C}$ electric field at a distance of 0.250 m ? (b) How large is the field at 10.0 m ? (OpenStax 18.30) $\mathbf{6 . 9 4} \times \mathbf{1 0}^{\mathbf{- 8}} \mathbf{C}, \mathbf{6 . 2 5} \mathrm{N} / \mathrm{C}$
9. (a) Find the direction and magnitude of an electric field that exerts a $4.80 \times 10^{-17} \mathrm{~N}$ westward force on an electron. (b) What magnitude and direction force does this field exert on a proton? (OpenStax 18.32) $\mathbf{3 0 0} \mathbf{N} / \mathrm{C}$ east, $\mathbf{4 . 8 0} \times \mathbf{1 0}^{\mathbf{- 1 7}} \mathbf{N}$ east
10. (a) Sketch the electric field lines near a point charge $+q$. (b) Do the same for a point charge $-3.00 q$. (OpenStax 18.33) see below
11. Sketch the electric field lines a long distance from the charge distributions shown in Figure 18.26 (a) and (b) (OpenStax 18.34) see below
12. The figure shows the electric field lines near two charges $q_{1}$ and $q_{2}$. What is the ratio of their magnitudes? (b) Sketch the electric field lines a long distance from the charges shown in the figure. (OpenStax 18.35) -1.9:1, like a point charge

13. Sketch the electric field lines in the vicinity of two opposite charges, where the negative charge is three times greater in magnitude than the positive. (See Figure 18.47 for a similar situation). (OpenStax 18.36)
(a)

$\qquad$

## Conductors in Equilibrium

- Conductors contain $\qquad$ charges that move $\qquad$
- When $\qquad$ charges are present, they quickly $\qquad$ to places where the electric field is to the surface
- Then they $\qquad$ moving
- This is electrostatic $\qquad$
- Conductor in electric field will $\qquad$
- Inside conductor, $\qquad$ -
$\qquad$ to $\qquad$

- Just outside of conductor, E-field is
- Any excess $\qquad$ resides on $\qquad$
- They get as far $\qquad$ as $\qquad$
- If the surface is $\qquad$ , more charge will collect near the area of most $\qquad$
- If the curve is great enough, the E-field can be $\qquad$ enough to $\qquad$
 excess charge


## Shielding

- A conductor $\qquad$ any charge $\qquad$ it from $\qquad$ electrical fields
- $\qquad$ electrical equipment is $\qquad$ by putting in a metal box called a $\qquad$ Cage
$\bullet$ $\qquad$ and $\qquad$ -


## Applications

- Copy Machine
- Laser Printer
- Ink Jet Printer


## Homework

1. Is the object in the figure a conductor or an insulator? Justify your answer.
2. If the electric field lines in the figure above were perpendicular to the object, would it necessarily be a conductor? Explain.

3. Why is a golfer with a metal club over her shoulder vulnerable to lightning in an open fairway? Would she be any safer under a tree?
4. Are you relatively safe from lightning inside an automobile? Give two reasons.
5. Considering the figure, suppose that $q_{a}=q_{d}$ and $q_{b}=q_{c}$. First show that $q$ is in static equilibrium. (You may neglect the gravitational force.) Then discuss whether the equilibrium is stable or unstable, noting that this may depend on the signs of the charges and the direction of displacement of $q$ from the center of the square.
6. If $q_{a}=0$ in the figure, under what conditions will there be no net Coulomb force on $q$ ?
7. Sketch the electric field lines in the vicinity of the conductor in the figure given the field was originally uniform and parallel to the object's long axis. Is the resulting field small near the long side of the object? (OpenStax 18.37) See other side

$\qquad$
8. Sketch the electric field between the two conducting plates shown in the figure, given the top plate is positive and an equal amount of negative charge is on the bottom plate. Be certain to indicate the distribution of charge on the plates. (OpenStax 18.39) See below

9. What is the force on the charge located at $x=8.00 \mathrm{~cm}$ in figure (a) given that $\mathrm{q}=1.00 \mu \mathrm{C}$ ? (OpenStax 18.41) 12.8 N
10. (a) Find the total electric field at $x=1.00 \mathrm{~cm}$ in figure (b) given that $\mathrm{q}=5.00 \mathrm{nC}$. (b) Find the total electric field at $\mathrm{x}=$ 11.00 cm in figure (b). (c) If the charges are allowed to move and eventually be brought to rest by friction, what will the
 final charge configuration be? (That is, will there be a single charge, double charge, etc., and what will its value(s) be?) (OpenStax 18.42) $-\infty, \mathbf{2 . 1 2} \times \mathbf{1 0}^{\mathbf{5}}$ N/C, $\boldsymbol{+ q}$
11. Using the symmetry of the arrangement, determine the direction of the force on $q$ in the figure below, given that $q_{a}=q_{b}=+7.50 \mu C$ and $q_{c}=q_{d}=-7.50 \mu C$. (b) Calculate the magnitude of the force on the charge $q$, given that the square is 10.0 cm on a side and $q=2.00 \mu C$. (OpenStax 18.45) down, 76.3 N downward

12. (a) Find the electric field at the location of $q_{a}$ in the figure if it is an equilateral triangle with sides 25 cm , given that $q_{b}=+10.00 \mu C$ and $q_{c}=-5.00 \mu C$. (b) What is the force on $q_{a}$, given that $q_{a}=$
 above the-x-axis

|  | $O_{q_{\mathrm{a}}}$ |  |
| :---: | :---: | :---: |
|  |  |  |
| $O_{q_{c}}$ |  | $O_{q_{0}}$ |

13. A simple and common technique for accelerating electrons is shown in the figure, where there is a uniform electric field between two plates. Electrons are released, usually from a hot filament, near the negative plate, and there is a small hole in the positive plate that allows the electrons to continue moving. (a) Calculate the acceleration of the electron if the field strength is $2.50 \times 10^{4} \mathrm{~N} / \mathrm{C}$. (b) Explain why the electron will not be pulled back to the positive plate once it moves through the hole. (OpenStax 18.53) $\mathbf{4 . 3 9 \times \mathbf { 1 0 } ^ { \mathbf { 1 5 } } \mathbf { ~ m } / \mathbf { s } ^ { \mathbf { 2 } } , \boldsymbol { E } = \mathbf { 0 } , 0}$


Answer to \#7
Answer to \#8

$\qquad$

## Electric Potential Energy

- Change in $\qquad$ due to $\qquad$
- Force of gravity is $\qquad$
- $F_{G}=G \frac{m_{1} m_{2}}{r^{2}}$
- $W=m g h_{0}-m g h_{f}=P E_{0}-P E_{f}$
- Change in $\qquad$ due to $\qquad$
- Electrical Force is $\qquad$
- $F_{E}=k \frac{q_{1} q_{2}}{r^{2}}$
- $W=P E_{0}-P E_{f}$


## Electric Potential (or Potential)

$$
V=\frac{E P E}{q_{0}}
$$

- Unit: $\qquad$ $(\mathrm{V}=\mathrm{J} / \mathrm{C})$

$$
\begin{aligned}
V_{f}-V_{0} & =\frac{P E_{f}}{q_{0}}-\frac{P E_{0}}{q_{0}}=-\frac{W}{q_{0}} \\
\Delta V & =\frac{\Delta P E}{q_{0}}=-\frac{W}{q_{0}}
\end{aligned}
$$

- $\quad V$ and EPE can only be measured in

Electric force moves a charge of $2 \times 10^{-10} \mathrm{C}$ from point A to point B and does $5 \times 10^{-6} \mathrm{~J}$ of work. What is the difference in potential energies of A and $\mathrm{B}\left(P E_{A}-P E_{B}\right)$ ?

What is the potential difference between A and $\mathrm{B}\left(V_{A}-V_{B}\right)$ ?

Electric Potential Difference and Charge Sign

- Positive Charge
- Moves from $\qquad$ electrical $\qquad$ toward $\qquad$ electrical potential
- Negative Charge
- Moves from $\qquad$ to $\qquad$ electrical potentials
Points A, B, and C are evenly spaced on a line. A positive test charge is released from A and accelerates towards B, from B it decelerates, but doesn't stop at C . What happens when a negative charge is released at B ?


## Batteries

- Even though it is the $\qquad$ electrons that actually $\qquad$ tradition says that we talk about
$\qquad$ _ charges
- Positive charge $\qquad$ by $\qquad$ terminal
- Moves through light bulb and $\qquad$ to heat
- By the time the $\qquad$ charge reaches the $\qquad$ terminal, it has no $\qquad$ energy left

$$
\begin{gathered}
V=\frac{E P E}{q_{0}} \\
E P E=q_{0} V
\end{gathered}
$$

- Use this when solving $\qquad$ of energy problems
- Unit for $\qquad$ energy is $\qquad$ (eV)

$$
e V=\left(1.60 \times 10^{-19} C\right)(1 V)=1.6 \times 10^{-19} J
$$

When lightning strikes, the potential difference can be ten million volts between the cloud and ground. If an electron is at rest and then is accelerated from the ground to the cloud, how fast will it be moving when it hits the cloud 0.5 km away (ignore relativity effects)?

## Homework

1. Voltage is the common word for potential difference. Which term is more descriptive, voltage or potential difference?
2. If the voltage between two points is zero, can a test charge be moved between them with zero net work being done? Can this necessarily be done without exerting a force? Explain.
3. What is the relationship between voltage and energy? More precisely, what is the relationship between potential difference and electric potential energy?
4. Voltages are always measured between two points. Why?
5. How are units of volts and electron volts related? How do they differ?
6. The drawing shows three possibilities for the potentials at two points, $A$ and $B$. In each case, the same positive charge is moved from $A$ to $B$. In which case, if any, is the most work done on the positive charge by the

| ${ }^{\text {a }}$ |  |  |  | ${ }^{\text {A }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 150 V | 100 V | 25 V | -25 V | -10 V | -60 v |
| Case 1 |  | Case 2 |  | Case 3 |  | electric force? Account for your answer.

7. Find the ratio of speeds of an electron and a negative hydrogen ion (one having an extra electron) accelerated through the same voltage, assuming non-relativistic final speeds. Take the mass of the hydrogen ion to be $1.67 \times 10^{-27} \mathrm{~kg}$. (OpenStax 19.1) 42.8
8. An evacuated tube uses an accelerating voltage of 40 kV to accelerate electrons to hit a copper plate and produce x-rays. Non-relativistically, what would be the maximum speed of these electrons? (OpenStax 19.2) $\mathbf{1 . 1 7 \times 1 0 ^ { \mathbf { 8 } } \mathbf { ~ m } / \mathbf { s } , ~}$
9. A bare helium nucleus has two positive charges and a mass of $6.64 \times 10^{-27} \mathrm{~kg}$. (a) Calculate its kinetic energy in joules at $2.00 \%$ of the speed of light. (b) What is this in electron volts? (c) What voltage would be needed to obtain this energy? (OpenStax 19.3) $\mathbf{1 . 2 0} \times \mathbf{1 0}^{-\mathbf{1 3}} \mathrm{J}, \mathbf{7 . 5 0} \times \mathbf{1 0}^{\mathbf{5}} \mathbf{e V}, \mathbf{3 . 7 5} \times \mathbf{1 0}^{\mathbf{5}} \mathrm{V}$
10. The temperature near the center of the Sun is thought to be 15 million degrees Celsius ( $1.5 \times 10^{7}{ }^{\circ} \mathrm{C}$ ). Through what voltage must a singly charged ion be accelerated to have the same energy as the average kinetic energy of ions at this temperature? (OpenStax 19.5) $\mathbf{1 . 9} \times \mathbf{1 0}^{\mathbf{3}} \mathrm{V}$
11. A lightning bolt strikes a tree, moving 20.0 C of charge through a potential difference of $1.00 \times 10^{2} \mathrm{MV}$. (a) What energy was dissipated? (b) What mass of water could be raised from $15^{\circ} \mathrm{C}$ to the boiling point and then boiled by this energy? (c) Discuss the damage that could be caused to the tree by the expansion of the boiling steam. (OpenStax 19.7) $\mathbf{2 . 0 0} \times \mathbf{1 0}^{9} \mathbf{~ J}$, 766 kg, BOOM!
$\qquad$

## Relation between E and V

Both electric $\qquad$ and electric $\qquad$ can be used to describe $\qquad$

- E
$\qquad$
deals with
○ $\qquad$
- V
- deals with $\qquad$
- $\qquad$


## Uniform Electric Field

$$
V_{A B}=E d \text { or } E=\frac{V_{A B}}{d}
$$

In general

$$
E=-\frac{\Delta V}{\Delta s}
$$

- E is gradient ( $\qquad$ ) of V vs. s ( $\qquad$ _)
- On picture, E-field lines show $\qquad$ . V lines are where V are $\qquad$

- The closer V $\qquad$ are, the $\qquad$ E is.
How far apart are two conducting plates that have an electric field strength of $4.50 \times 10^{3} \mathrm{~V} / \mathrm{m}$ between them, if their potential difference is 15.0 kV ?


A doubly charged ion is accelerated to an energy of 15.0 keV by the electric field between two parallel conducting plates separated by 3.00 mm . What is the electric field strength between the plates?

## Homework

1. Discuss how potential difference and electric field strength are related. Give an example.
2. What is the strength of the electric field in a region where the electric potential is constant?
3. Will a negative charge, initially at rest, move toward higher or lower potential? Explain why.
4. Show that units of $\mathrm{V} / \mathrm{m}$ and $\mathrm{N} / \mathrm{C}$ for electric field strength are indeed equivalent. (OpenStax 19.13)
5. What is the strength of the electric field between two parallel conducting plates separated by 1.00 cm and having a potential difference (voltage) between them of $1.50 \times 10^{4} \mathrm{~V}$ ? (OpenStax 19.14) $\mathbf{1 . 5 0} \times \mathbf{1 0}^{\mathbf{6}} \mathbf{~ V} / \mathbf{m}$
6. The electric field strength between two parallel conducting plates separated by 4.00 cm is $7.50 \times 10^{4} \mathrm{~V} / \mathrm{m}$. (a) What is the potential difference between the plates? (b) The plate with the lowest potential is taken to be at zero volts. What is the potential 1.00 cm from that plate (and 3.00 cm from the other)? (OpenStax 19.15) $3.00 \mathrm{kV}, 750 \mathrm{~V}$
7. How far apart are two conducting plates that have an electric field strength of $4.50 \times 10^{3} \mathrm{~V} / \mathrm{m}$ between them, if their potential difference is 15.0 kV ? (OpenStax 19.16) 3.33 m
8. The voltage across a membrane forming a cell wall is 80.0 mV and the membrane is 9.00 nm thick. What is the electric field strength? (The value is surprisingly large, but correct.) You may assume a uniform electric field. (OpenStax 19.18) $8.89 \times 10^{6} \mathrm{~V} / \mathrm{m}$
9. Membrane walls of living cells have surprisingly large electric fields across them due to separation of ions. What is the voltage across an 8.00 nm -thick membrane if the electric field strength across it is $5.50 \mathrm{MV} / \mathrm{m}$ ? You may assume a uniform electric field. (OpenStax 19.19) $\mathbf{4 4 . 0} \mathbf{~ m V}$
10. A doubly charged ion is accelerated to an energy of 32.0 keV by the electric field between two parallel conducting plates separated by 2.00 cm . What is the electric field strength between the plates? (OpenStax 19.22) $\mathbf{8 . 0 0} \times \mathbf{1 0} \mathbf{~} \mathbf{V} / \mathbf{m}$
11. An electron is to be accelerated in a uniform electric field having a strength of $2.00 \times 10^{6} \mathrm{~V} / \mathrm{m}$. (a) What energy in keV is given to the electron if it is accelerated through 0.400 m ? (b) Over what distance would it have to be accelerated to increase its energy by 50.0 GeV ? (OpenStax 19.23 ) $\mathbf{8 0 0} \mathbf{~ k e V , ~} \mathbf{2 5 . 0} \mathbf{~ k m}$
$\qquad$

## Electric Potential of a Point Charge

$$
V=\frac{k q}{r}
$$

- V is $\qquad$ the $\qquad$ potential
- V $\qquad$ the potential difference if a test charge were $\qquad$ to a distance of $r$ from
- Two or more charges
- Find the $\qquad$ due to $\qquad$ charge at that location

the potentials together to get the $\qquad$ potential
Two charges are 1 m apart. The charges are $+2 \mu \mathrm{C}$ and $-4 \mu \mathrm{C}$. What is the potential $1 / 3$ of the way between them?

How much work is done $\left(-W=P E_{f}-P E_{0}\right)$ to bring two electrons to a distance of $5.3 \times 10^{-11} \mathrm{~m}$ to the nucleus of a Helium atom $\left(q=3.2 \times 10^{-19} C\right)$ ?

## Equipotential Lines

- Lines where the electric $\qquad$ is the $\qquad$
- Perpendicular to $\qquad$
- No $\qquad$ is required to move charge along $\qquad$ line since $q \Delta V=0$
Sketch the equipotential lines in the vicinity of two opposite charges, where the negative charge is three times as great in magnitude as the positive.



## Homework

1. What is an equipotential line? What is an equipotential surface?
2. Explain in your own words why equipotential lines and surfaces must be perpendicular to electric field lines.
3. Can different equipotential lines cross? Explain.
4. Imagine that you are moving a positive test charge along the line between two identical point charges. With regard to the electric potential, is the midpoint on the line analogous to the top of a mountain or the bottom of a valley when the two point charges are (a) positive and (b) negative? Explain.
5. The potential at a point in space has a certain value, which is not zero. Is the electric potential energy the same for every charge that is placed at that point? Explain.
6. What is the potential $0.530 \times 10^{-10} \mathrm{~m}$ from a proton (the average distance between the proton and electron in a hydrogen atom)? (OpenStax 19.25) 27.2 V
7. (a) A sphere has a surface uniformly charged with 1.00 C . At what distance from its center is the potential 5.00 MV ? (b) What does your answer imply about the practical aspect of isolating such a large charge? (OpenStax 19.26) $1.80 \mathbf{k m}$
8. How far from a $1.00 \mu \mathrm{C}$ point charge will the potential be 100 V ? At what distance will it be $2.00 \times 10^{2} \mathrm{~V}$ ? (OpenStax 19.27) $\mathbf{9 0 . 0} \mathbf{~ m}, 45.0 \mathrm{~m}$
9. What are the sign and magnitude of a point charge that produces a potential of -2.00 V at a distance of 1.00 mm ? (OpenStax 19.28) - $\mathbf{2 . 2 2 \times 1 0 ^ { - 1 3 }} \mathbf{C}$
10. In nuclear fission, a nucleus splits roughly in half. (a) What is the potential $2.00 \times 10^{-14} \mathrm{~m}$ from a fragment that has 46 protons in it? (b) What is the potential energy in MeV of a similarly charged fragment at this distance? (OpenStax 19.30)

## $3.31 \times 10^{6} \mathrm{~V}, 152 \mathrm{MeV}$

11. (a) What is the potential between two points situated 10 cm and 20 cm from a $3.0 \mu \mathrm{C}$ point charge? (b) To what location should the point at 20 cm be moved to increase this potential difference by a factor of two? (OpenStax 19.34) $\mathbf{1 3 5} \times \mathbf{1 0}^{\mathbf{3}} \mathrm{V}$, $\infty$
12. (a) Sketch the equipotential lines near a point charge $+q$. Indicate the direction of increasing potential. (b) Do the same for a point charge $-3 q$. (OpenStax 19.36)
13. Sketch the equipotential lines for the two equal positive charges shown in the figure. Indicate the direction of increasing potential. (OpenStax 19.37)

14. The figure below shows the electric field lines near two charges $q_{1}$ and $q_{2}$, the first having a magnitude four times that of the second. Sketch the equipotential lines for these two charges, and indicate the direction of increasing potential.
(OpenStax 19.38)
15. Sketch the equipotential lines a long distance from the charges shown in the figure below. Indicate the direction of increasing potential. (OpenStax 19.39)



## Physics

1. What is the charge of an electron?
2. What is the value of $k$ ?
3. What are some combinations of charges that attract? Repel?
4. Know the steps to charge by contact and by induction.
5. Definitions: electric potential difference, electric potential energy, equipotential lines, electric field, electric field lines, conductors, insulators
6. Is electric force conservative?
7. A piece of wire has a charge of $-3.2 \times 10^{-5}$ C. How many extra electrons does it have?
8. At what separation will two charges, each of magnitude $10.0 \mu \mathrm{C}$, exert a force of 5 N on each other?
9. A $-10.0-\mu C$ charge is located 0.50 m to the right of $a+15.0-\mu \mathrm{C}$ charge. What is the magnitude and direction of the electrostatic force on the positive charge?
10. Know about the electric field in a parallel plate capacitor.
11. How is the spacing of the electric field lines related to the strength?
12. How is the number of electric field line related to the size of the charge?
13. Where are the excess charges on a conductor located?
14. What is the magnitude and direction of the electric force on $a+5 \mu C$ charge at a point where the electric field is $5000 N / C$ and is directed on the $-x$ axis?
15. The electric potential at a certain point in space is 6 V . What is the electric potential energy of a -4 C charge placed at that point in space?
16. If a 2-C charge is located at the origin and a-3-C charge is located at $x=2 m$, where is the electric potential zero?
17. If the work required to move a -0.25 C charge from point $A$ to point $B$ is +100 J , what is the potential difference between the two points? What is the difference in potential energies of $A$ and $B$ ?
18. Given a picture of equipotential lines, be able to find area of greatest electric potential energy and electric field strength.
19. $-1.60 \times 10^{-19} \mathrm{C}$
20. $8.99 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}}$
21. Attract:,$+-;+, 0 ;-, 0 ;$ Repel: + , +; -, -
22. See textbook or notes
23. $\frac{-3.2 \times 10^{-5} C}{-1.60 \times 10^{-19} C}=\mathbf{2 . 0} \times \mathbf{1 0}^{\mathbf{1 4}}$ electrons
24. $F=k \frac{\left|q_{1} q_{2}\right|}{r^{2}}$
$5 \mathrm{~N}=\left(8.99 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}}\right) \frac{\left|\left(10 \times 10^{-6} \mathrm{C}\right)\left(10 \times 10^{-6} \mathrm{C}\right)\right|}{r^{2}}$
$r^{2}=\left(8.99 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}}\right) \frac{\left|\left(10 \times 10^{-6} \mathrm{C}\right)\left(10 \times 10^{-6} \mathrm{C}\right)\right|}{5 \mathrm{~N}}$
$r^{2}=0.1798 m^{2}$
$\boldsymbol{r}=0.424 \mathrm{~m}$
25. $F=k \frac{\left|q_{1} q_{2}\right|}{r^{2}}$
$F=\left(8.99 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}}\right) \frac{\left|\left(-10 \times 10^{-6} \mathrm{C}\right)\left(15 \times 10^{-6} \mathrm{C}\right)\right|}{(0.5 \mathrm{~m})^{2}}$
$F=5.39 \mathrm{~N}$ to the right
26. Constant, etc.
27. Wider space, less field
28. More lines, more charge
29. On surface
30. $E=\frac{F}{q}$
$-5000 \frac{N}{C}=\frac{F}{5 \times 10^{-6} \mathrm{C}}$
$F=-0.025 \mathrm{~N}$
$0.025 N$ in the $-x$ direction
31. $V=\frac{E P E}{q_{0}}$
$6 V=\frac{E P E}{-4 C}$
$E P E=-24 J$
32. $V=\frac{k Q}{r}$
$\frac{k(2 C)}{x}+\frac{k(-3 C)}{2-x}=0$
$\frac{(2-x) k(2 C)}{x(2-x)}+\frac{x k(-3 C)}{x(2-x)}=0$
$(2-x)(2 C)+x(-3 C)=0$
$4 C-(2 C) x-(3 C) x=0$
$4 C=(5 C) x$
$\boldsymbol{x}=0.8 \mathrm{~m}$
33. $V_{B}-V_{A}=\frac{E P E_{B}}{q_{0}}-\frac{E P E_{A}}{q_{0}}=\frac{-W_{A B}}{q_{0}}$
$V_{B}-V_{A}=\frac{-W_{A B}}{q_{0}}$
$V_{B}-V_{A}=\frac{-100 \mathrm{~J}}{-0.25 \mathrm{C}}=400 \mathrm{~V}$
$W_{A B}=-W_{B A}=-100 \mathrm{~J}$
34. EPE: electron has highest EPE at lowest $V$ and proton has highest EPE at highest $V$
E-field: highest at place where equipotential lines are closest together
